Integrated Polarization Analyzing CMOS Image Sensor for Material Classification

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Abstract—Material classification is an important application in computer vision. The inherent property of materials to partially polarize the reflected light can serve as a tool to classify them. In this paper, a real-time polarization sensing CMOS image sensor using a wire grid polarizer is proposed. The image sensor consists of an array of 128 × 128 pixels, occupies an area of 5 × 4 mm² and it has been designed and fabricated in a 180-nm CMOS process. We show that this image sensor can be used to differentiate between metal and dielectric surfaces in real-time due to the different nature in partially polarizing the specular and diffuse reflection components of the reflected light. This is achieved by calculating the Fresnel reflection coefficients, the degree of polarization and the variations in the maximum and minimum transmitted intensities for varying specular angle of incidence. Differences in the physical parameters for various metal surfaces result in different surface reflection behavior, influencing the Fresnel reflection coefficients. It is also shown that the image sensor can differentiate among various metals by sensing the change in the polarization Fresnel ratio.

Index Terms—degree of polarization, Fresnel reflection coefficients, image sensor, material classification, polarization, stokes parameters, wire grid polarizer.

I. INTRODUCTION

A. Material Classification

INFORMATION on the type of material can provide important information about the scene in computer or machine vision applications. Materials can be broadly classified into metals and dielectrics, based on their conductivity. Metals are highly conductive, opaque, and tend to be very reflective while dielectrics are less conductive and have very low reflectivity.

Earlier attempts to distinguish between metals and dielectrics used the dichromatic reflection properties of the material surface [1]–[3]. Materials were classified into optically homogenous or optically inhomogeneous. Healey [4] showed that homogenous materials reflect light only from the surface. Thus, when such materials are illuminated with a monochromatic light beam they reflect light of a fixed color (wavelength). Inhomogeneous materials on the other hand reflect light from the surface and also scatter light from the body. Such a material, when illuminated with a monochromatic light beam would reflect two distinct colors, one being the reflected color from the surface while the other being the color of the light scattered from the body. Based on the number of reflected colors the objects can be classified as homogenous or inhomogeneous. Once the object has been determined to be either homogenous or inhomogeneous, it can be further classified as a metal or a dielectric depending on the reflected color. Metals have free electrons, and when these electrons are hit by a light ray the resulting response of the electrons is a function of the wavelength of the light ray. Some metals such as steel and nickel produce near uniform response for changes in the wavelength over the entire visible spectrum while certain metals such as copper and gold tend to reflect longer wavelengths more than the shorter ones. Dielectrics on the other hand do not have free electrons thus the reflectivity from a dielectric surface is independent of the wavelength of the incident light ray. This method, however, is limited by the distortion of the color histogram obtained after reflection, which depends on the object geometry. Additionally, the color of the material also influences the reflected color.

Another method to discriminate between metals and dielectrics is based on the Fresnel reflection theory which was proposed by Wolff [5], [6]. According to this theory, dielectric surfaces polarize the light upon specular reflection stronger than metal surfaces for all angles of incidence. The Fresnel reflection coefficients are used to compute the polarization Fresnel ratio (PFR), which is shown to be equal to the ratio of the maximum to the minimum transmitted irradiance at the material surface [5]. The PFR is used to classify materials into metals and dielectrics. The maximum and minimum transmitted irradiances are obtained by allowing the reflected light from the material surface to pass through an external linear polarizer onto a CCD or CMOS image sensor. The disadvantage of such a system is that the linear polarization filters have to be externally controlled, which complicates the automation and miniaturization of optical sensors for material classification.

Additionally, the PFR is computed using digital processing blocks which increase the overall power consumption of the system.

B. Polarization Image Sensors

State-of-the-art of polarization image sensors consists of either a standard CMOS/CCD camera coupled with an external sensor for material classification.
polarization filter, or on integrated polarization filters fabricated on top of the pixel array. The latter can measure polarization information in real time.

From the aperture theory [7], [8], it is known that for an electromagnetic wave to be absorbed by a wire grid, its wavelength should be larger than the pitch of the wire grid (\( \lambda / d > 2 \)); where \( \lambda \) is the wavelength and \( d \) is the spacing between the wire grid). To obtain the polarization information in the visible spectrum, a wire grid pitch of less than 300 nm is desired. With the scaling of CMOS technologies, the minimum distance between metal wires also scales, opening up the possibility of using them in a grid structure for the absorption of electromagnetic waves, thus polarizing the transmitted wave. An embedded wire grid polarizer with an extinction ratio of 2.03 has already been demonstrated [9], [10]. The wire grid pitch used was 1.2 \( \mu \)m. An integrated polymer polarization filter array with a pitch of 6 \( \mu \)m has also been reported [11].

In this paper, we present a CMOS image sensor with real time polarization sensing ability using a metal wire grid pitch of 0.48 \( \mu \)m. The image sensor uses the model proposed in [5] and [6] to classify materials based on the polarization information.

The theory behind Fresnel coefficients is covered in Section II. In Section III, the CMOS image sensor is described. Section IV presents the measured transmittance of the wire grid polarizer. Section V describes the methods for material classification. Section VI concludes the paper and outlines the future work.

II. THEORY

A. Polarization and Fresnel Coefficients

Electromagnetic radiation travels as transverse waves, i.e., waves that vibrate in a direction perpendicular to their direction of propagation. Polarization is a phenomenon peculiar to transverse waves based on the distribution of the electric field in the plane normal to the propagation direction. In an unpolarized or randomly polarized electromagnetic wave the orientation of the electric vector changes randomly.

A mathematical representation of a plane wave propagating in the \( z \) direction is given as

\[
E = E_0 \cos(kz - \omega t + \varphi_0)
\]

(1)

where \( E_0 \) is the amplitude, \( k \) is the propagation (or wave) constant \( (k = 2\pi / \lambda) \), \( \omega \) is the circular frequency \( (\omega = kc = 2\pi c / \lambda) \), and \( \varphi_0 \) is the initial phase.

An unpolarized electromagnetic wave can be polarized through absorption, reflection, refraction, and scattering. In this paper, we will focus our discussion to polarization of electromagnetic waves by reflection. The polarization by reflection from a material surface depends on the angle at which the light strikes the reflecting surface as well as on the nature of said surface. Metallic surfaces reflect light with a variety of vibration directions, and such reflected light is usually unpolarized. However, nonmetallic surfaces reflect light such that the vibrations of the reflecting light wave is parallel to the plane of the reflecting surface.

Polarization can either be elliptical, circular or linear in nature. Elliptical polarized light consists of two perpendicular waves of unequal amplitude which differ in phase by 90°. If the perpendicular waves are of equal amplitude it results in a circularly polarized light. A linearly polarized wave has its electric field vibrating in the same direction at all times at a particular point. Elliptical and circular polarizations are more uncommon in nature than linear polarization. Furthermore, since a wire grid allows only a specific polarization to pass through, the transmitted wave will have a single linear polarization and thus only the linear polarization in considered in this work.

When a light ray strikes a surface, part of the incident light is reflected and part is transmitted or absorbed as shown in Fig. 1, \( \varphi \) is the angle of incidence of the incident ray, \( \varphi' \) is the angle of reflection of the reflected ray and \( \eta \) is the angle of transmission of the transmitted ray.

The reflection occurring at the surface of the planar surface can be divided into diffuse and specular. When light strikes a surface, part of the light passes through the boundary, which is re-emitted randomly. Diffuse reflection is caused by the reflected rays from internal scattering inside the surface medium. The diffuse reflection component is independent of the angle of reflection but depends on the angle of incidence.

Specular reflection is a mirror-like reflection from the surface, in which light from a single incoming direction is reflected into a single outgoing direction. Pure specular reflection occurs when the planar interface portion of the surface is significantly larger than the wavelength of the incident light [5]. The incident and the reflected directions of the specularly reflected light determine the specular plane of incidence.

Unpolarized light becomes partially polarized after specular reflection. The incident electric field can be split into two components, one perpendicular to the plane of incidence with amplitude \( E_p \) and the other parallel to the plane of incidence with amplitude \( E_s \), as shown in Fig. 1. When the incident transverse wave reaches the boundary between the mediums, it is divided into a reflected and a refracted wave component. The fraction of the incident light that is reflected from the interface is given by the reflection coefficients \( R \), and the fraction that is refracted is given by the refraction coefficients \( D \). Since the incident light has polarized components, the reflected and the refracted light will also have polarized components which are expressed in

![Fig. 1. Incident, reflected, and transmitted Fresnel coefficients.](image-url)
terms of the Fresnel reflection coefficients. The Fresnel reflection equations are expressed as

\[
\begin{align*}
R_p &= -E_p \frac{\sin(\varphi - \eta)}{\sin(\varphi + \eta)} \\
R_s &= -E_s \frac{\tan(\varphi - \eta)}{\tan(\varphi + \eta)} \\
D_s &= E_s \frac{2 \sin \eta \cos \varphi}{\sin(\varphi + \eta)} \\
D_p &= E_p \frac{2 \sin \eta \cos \varphi}{\sin(\varphi + \eta) \cos(\varphi - \eta)}.
\end{align*}
\] (2)

\(R_p, R_s, D_p,\) and \(D_s\) are the reflection and refraction coefficients, \(\varphi\) is the angle of reflection, and \(\eta\) is the angle of refraction.

The Fresnel coefficients are used to describe the amount of light reflected or transmitted from a surface and form the basis of Fresnel reflectance model discussed in Section II-B. The polarization of the light wave expressed by (1) and also the polarized reflected and transmitted components in (2) describe the polarization in terms of its amplitude. The amplitude of the optical field cannot be observed, but it is possible to observe and measure the intensity which is the time average of the square of the field amplitudes. The Stokes parameters which are used to represent the polarization in terms of the intensity of the light wave are discussed further in Section II-C.

B. Fresnel Reflectance Model

The reflectance model describes the intensity and spectral composition of the light reflected from the reflectance surface and reaching the observer. The intensity of the reflected light depends on the intensity and size of the light source and also on the surface properties of the material. The spectral composition of the reflected light is determined by the wavelength selective reflection of the surface.

When the reflected wave component is passed through a linear polarizer, the intensity of the image can be expressed as a function of the transmission axis of the polarizer \((\theta)\) [5]. The spectral transmittances of the polarizer for linearly polarized light and unpolarized light are denoted by \(T_p(\lambda)\) and \(T_n(\lambda)\), respectively, where \(\lambda\) is the wavelength of the light.

The intensity image of the reflected light from the surface is expressed in terms of the pixel coordinates \((x, y)\) and the transmission axis of the polarizer. The intensity image obtained after the reflection can be written as a sum of the diffuse reflection coefficient \(I_d(x, y)\) and the specular reflection coefficient \(I_s(x, y)\) [5], [13]. Using the Fresnel reflection (2), the intensity image observed through the polarizer transmission axis \(\theta\) can be expressed as shown in (3) at the bottom of the page, where \(\theta_0\) is the direction perpendicular to the specular plane. The Fresnel reflection coefficients \(R_p\) and \(R_s\) depend on the pixel coordinates. In terms of polarized and unpolarized components, (3) can be rewritten as

\[
I(x, y : \theta) = A(x, y) \frac{1 + \cos^2(\theta - \theta_0)}{2} + B(x, y)
\] (4)

where

\[
A(x, y) = \frac{R_p(x, y) + R_s(x, y)}{R_p(x, y) + R_s(x, y)} T_p I_s(x, y)
\] (5)

\[
B(x, y) = \frac{R_p(x, y)}{R_p(x, y) + R_s(x, y)} T_p I_s(x, y) + T_n I_d(x, y)
\] (6)

It can be observed from (4) that \(I(x, y : \theta)\) oscillates as \(\theta\) varies between the maximum \(I_{\max}(x, y)\) at \(\theta = \theta_0 \pm \pi/2\) and the minimum \(I_{\min}(x, y)\) at \(\theta = \theta_0 \pm \pi/2\). \(I_{\max}(x, y)\) and \(I_{\min}(x, y)\) are then expressed in terms of (5) and (6) as

\[
I_{\max}(x, y) = A(x, y) + B(x, y)
\]

\[
= \frac{R_p(x, y) + R_s(x, y)}{R_p(x, y) + R_s(x, y)} T_p I_s(x, y) + T_n I_d(x, y)
\] (7)

\[
I_{\min}(x, y) = B(x, y)
\]

\[
= \frac{R_p(x, y)}{R_p(x, y) + R_s(x, y)} T_p I_s(x, y) + T_n I_d(x, y)
\] (8)

The first term in (4) is the polarized component of the reflection mainly contributed by the specular reflection of the incident transverse wave. The second term represents the unpolarized component contributed by the diffuse reflections and partly by the specular reflection which is not polarized.

C. Stokes Parameters and Degree of Polarization

The polarization state of an electromagnetic wave can be conveniently described by the Stokes parameters. These parameters were developed in 1852 by G. G. Stokes and are widely used to represent the partial polarization states. The four Stokes parameters are grouped into the Stokes vector as shown as

\[
\mathbf{S} = \begin{bmatrix}
S_0 \\
S_1 \\
S_2 \\
S_3
\end{bmatrix} = \begin{bmatrix}
I \\
Q \\
U \\
V
\end{bmatrix}.
\] (9)

The Stokes parameters represented in (9) are intensity \((I)\), degree of polarization \((Q)\), plane of polarization \((U)\), and ellipticity \((V)\).

The vector components are given by

\[
S_0 = E_{x0}^2 + E_{y0}^2
\]

\[
S_1 = E_{x0}^2 - E_{y0}^2
\]

\[
S_2 = 2E_{x0}E_{y0} \cos(\varphi)
\]

\[
S_3 = 2E_xE_y \sin(\varphi)
\] (10)

\[
I(x, y : \theta) = T_n I_d(x, y) + T_p \frac{R_p(x, y) \sin^2(\theta - \theta_0) + R_s(x, y) \cos^2(\theta - \theta_0)}{R_p(x, y) + R_s(x, y)} \times I_s(x, y)
\] (3)
where $E_{||}$ is the field strength of parallel polarized light, $E_{\perp}$ is the field strength of perpendicular polarized light, and $\Delta \phi$ is the phase difference between the parallel and perpendicular polarized light.

There are two ways to express the partial polarization: the degree of polarization (DOP) and the Jones coherency matrix $J$ [12]. The degree of polarization is a measure of the percentage of the electric field of light which is polarized compared to the electric field of total incident light. DOP is a scalar value between 0 and 1, and will be used to express the partial polarization in this work [12], [14]. In terms of Stokes parameters, the degree of polarization (DOP) of the light beam is expressed as

$$DOP = \delta = \frac{\sqrt{S_1^2 + S_2^2 + S_3^2}}{S_0}. \quad (11)$$

Three states of polarization of a light wave are possible: completely unpolarized, completely polarized, or partially polarized. A completely polarized light in terms of Stokes parameters is represented by $S_0^2 = S_1^2 + S_2^2 + S_3^2$ and a DOP of 1. For a completely unpolarized light, the Stokes parameters satisfy $S_1 = S_2 = S_3 = 0$ and $DOP = 0$. A partially polarized light satisfies $S_0^2 > S_1^2 + S_2^2 + S_3^2$.

In a linearly polarized light beam, circular and elliptical polarizations do not usually occur, its degree of polarization is thus often referred to as degree of linear polarization. The degree of linear polarization (DOLP) of a light beam is defined by

$$DOLP = \frac{S_1}{S_0}. \quad (12)$$

III. SENSOR DESCRIPTION

The image sensor consists of an array of 128 by 128 pixels, it occupies an area of $5 \times 4 \text{ mm}^2$ and it has been designed and fabricated in the 180-nm CMOS CIS process from UMC. The sensor has an embedded linear wire grid polarizer in each pixel, realized with the first metal layer of the process on top of a pinned photodiode ($p^+/n^+/p$-sub). The linear wire grid polarizer was implemented using thin metal strips with a line/space of 240 nm/240 nm (pitch of 480 nm) as shown in Fig. 2. Although

![Wire grid polarizer](image)

**Fig. 2. Wire grid polarizer.**

A pitch of less than 300 nm is required to cover the complete visible spectrum wavelength range, the chosen technology allows only for a pitch of 480 nm.

**Fig. 3 shows the sensor architecture.**

**Table I**

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Process</td>
<td>0.18µm 1 poly 3 metals UMC CIS process</td>
</tr>
<tr>
<td>On-chip Polarizer</td>
<td>Line/Space = 240nm/240nm (480nm pitch)</td>
</tr>
<tr>
<td>Active imager size</td>
<td>3.2 mm(H) x 3.2 mm(V)</td>
</tr>
<tr>
<td>Chip Size</td>
<td>4 mm(H) x 5 mm(V)</td>
</tr>
<tr>
<td>Active pixels</td>
<td>128 x 128</td>
</tr>
<tr>
<td>Pixel size</td>
<td>25µm x 25µm</td>
</tr>
<tr>
<td>Shutter type</td>
<td>Global shutter</td>
</tr>
<tr>
<td>Maximum data rate/master clock</td>
<td>64 MPS / 32 MHz</td>
</tr>
<tr>
<td>Supply voltage</td>
<td>1.8V</td>
</tr>
</tbody>
</table>

The chip is divided into four main blocks: the pixel array, the analog readout, the digital readout and the row select logic and timing control. The pixel array with the photodiodes and the associated circuitry for analog computations occupies most of the chip area. Each pixel contains a pinned photodiode and 32 transistors to perform low level image processing. In this paper we focus on the polarization sensing ability of the designed image sensor and thus the low level image processing will not be discussed.

The size of the photodiode is 10 µm x 10 µm which corresponds to a 16% pixel fill factor. Placed below the pixel array is the analog readout circuit, which consists of column level circuits (double differential sampling circuit), an output amplifier, a buffer and the column shift register. Placed at the top is the digital readout circuit, which consists of a 7-bit counter and a column shift register. The 7-bit counter is used to count the number of active high pixels in each row. Finally, the left side is dedicated to a row select logic and timing control blocks to address each row of pixels sequentially.

The array of 128 by 128 pixels was split into three regions as shown in Fig. 4.

1) A $64 \times 128$ array without a metal grid used for normal imaging applications.
2) A $64 \times 64$ array (sense region 1) consisting of 2 by 2 pixel arrays where two pixels (A and B) measure the intensity while the other two measure the $0^\circ$ (D), and $90^\circ$ (C) polarized intensity, respectively.

3) A $64 \times 64$ array (sense region 2) consisting of 2 by 2 pixel arrays where one pixel records the intensity of the light (A) while the other 3 record the $0^\circ$ (B), $45^\circ$ (C) and $90^\circ$ (D) polarized intensity.

The additional pixel sensitivity to $45^\circ$ polarized light in sense region 2 is used to compute the Stokes parameters. The pixels dedicated to sense the intensity in regions 1 and 2 are used to normalize the data obtained from the pixels sensitive to polarization directions.

IV. TRANSMITTANCE MEASUREMENTS

Linear polarizers are characterized by two main specifications: transmittance and contrast or extinction ratio. The transmittance is the percentage of light that passes through the linear polarizer. The contrast or extinction ratio is defined as the ratio of the power of a plane-polarized beam that is transmitted through a polarizer placed in its path with its polarizing axis parallel to the plane of the beam, as compared with the transmitted power when the polarizer axis is perpendicular to the plane of the beam.

In order to characterize the sensor, we used a polarized light obtained by passing the light from a dc light source through a linear polarizer. The transmission axis of the linear polarizer is varied from $0^\circ$ to $180^\circ$ in steps of $15^\circ$ to change the polarization angle of the light reaching the image sensor. The corresponding analog output of the pixels sensitive to $0^\circ$ and $90^\circ$ in the polarization sense region 1 and $0^\circ$, $45^\circ$, and $90^\circ$ in the polarization sense region 2 are stored. The obtained analog output is normalized with respect to the intensity obtained at the intensity sensitive pixel. The normalized output is the transmittance of the wire grid polarizer.

The normalized transmittance as a function of the transmission axis of the linear polarizer (incident polarization angle) for the two polarization sense regions are shown in Fig. 5.

The transmitted radiance of a linearly polarized light beam varies sinusoidally as function of the polarizer transmission axis. The maximum $I_{\text{MAX}}$, of the sinusoid occurs when the polarizer orientation is parallel to the orientation of the linear polarized component and the minimum $I_{\text{MIN}}$ occurs when the polarizer orientation is perpendicular to the linear polarized component. The mean maximum ($T_{\text{MAX}}$) and minimum ($T_{\text{MIN}}$) transmittances for $0^\circ$ and $90^\circ$ polarization sensitive pixels in the polarization region 1 and 2 are shown in Table II.

The maximum and the minimum transmittance for the $45^\circ$ sensitive pixel are 0.446 and 0.02, respectively.

V. MATERIAL CLASSIFICATION

A. Measurement Setup

The measurement setup for the measurements of the maximum and minimum transmitted intensities after reflection from the material surface is shown in Fig. 6. The polarized electromagnetic waves are reflected from the surface. At the boundary of the reflection surface, both the diffuse component and the specular component of the reflection of
the incident light are present. These reflection components are then incident on the image sensor after focusing by a lens. The analog signal from the image sensor is digitized using an external ADC and then analyzed using a PC. For the first version the analysis was done off-chip to prove the concept. The transmission axis of the linear polarization filter is varied from 0° to 90° in steps of 30° to change the polarization angle of the light reflected by the reflection surface.

At the beginning of the experiment the mean of the chosen pixel array of 20 × 20 without the linear polarizer is noted as in (13), which is used as a normalization factor:

\[ P_{\text{avg(with linear polarizer)}}(x, y) = \frac{1}{XY} \sum_{n=1}^{N} \sum_{x=0}^{X-1} \sum_{y=0}^{Y-1} p_n(x, y) \]

where \( X \) and \( Y \) are the pixel array dimensions and \( N \) is the total number of frames used to compute the mean. The normalized intensity is then obtained by dividing the mean pixel intensity with the linear polarizer (13) by the mean pixel intensity without the linear polarizer (14) shown in (15).

The mean of the acquired intensity values of the pixels sensitive to 0° and 90° in sense region 1, and of the pixels sensitive to 0°, 45°, and 90° in sense region 2, is computed for 30 frames as follows:

\[ P_{\text{avg(with linear polarizer)}}(x, y) = \frac{1}{N} \sum_{n=1}^{N} p_n(x, y) \]

where \( p(x, y) \) is the measured pixel intensity, \( x \) and \( y \) are the row and column number of the sensor array, and \( N \) is the number of frames selected:

\[ \text{Normalized } p_{\text{avg}}(x, y) = \frac{1}{N} \sum_{n=1}^{N} p_n(x, y) \]

\[ = \frac{1}{XY} \sum_{n=1}^{N} \sum_{x=0}^{X-1} \sum_{y=0}^{Y-1} p_n(x, y) \]

\[ = \frac{N}{X} \sum_{n=1}^{N} \frac{1}{Y} \sum_{x=0}^{X-1} \sum_{y=0}^{Y-1} p_n(x, y) \]

\[ (15) \]

B. Polarization Transmittance

The magnitude of oscillations of the reflected irradiance of the light after reflection is larger for dielectrics than for metals [5]. The intensity of the reflected wave is a function of the transmission axis of the linear polarizer \( I(x, y : \theta) \) and oscillates between the maximum transmitted intensity \( I_{\text{max}} \) and the minimum transmitted intensity \( I_{\text{min}} \) as shown in (4). For dielectrics the Fresnel coefficients satisfy \( R_p \gg R_s \) while for metals \( R_p \approx R_s \). The diffuse component of reflection dominates over the specular component \( I_d(x, y) \gg I_s(x, y) \) for dielectrics and thus the oscillations given by (7) and (8) vary over a larger range, while in case of metals, the oscillations are relatively smaller as the specular component of reflection dominates over the diffuse component of reflection \( I_s(x, y) \gg I_d(x, y) \).

Fig. 7 shows the measured transmitted irradiance in the sense regions 1 and 2 for 0° and 90° sensitive pixels for aluminum and plastic reflecting surface.

The differences between the maximum and minimum transmitted irradiances for plastic and aluminum surfaces in both regions 1 and 2 are shown in Table III.

<table>
<thead>
<tr>
<th>TABLE III</th>
</tr>
</thead>
<tbody>
<tr>
<td>TRANSMITTED IRADIANCE FOR PLASTIC AND ALUMINUM</td>
</tr>
<tr>
<td>Region 1</td>
</tr>
<tr>
<td>Plastic</td>
</tr>
<tr>
<td>( I_{\text{max}}(0°) )</td>
</tr>
<tr>
<td>( I_{\text{max}}(90°) )</td>
</tr>
</tbody>
</table>

Fig. 7. Transmitted Intensity at 0° and 90° polarization sensitive pixel in sense region 1 (top) and sense region 2 (bottom).
1 and 2 are much higher than those for aluminum. The differences in the transmitted irradiance are due to the difference in the reflection pattern of the light from the aluminum and plastic surfaces.

C. Material Classification Using the DOP

The light reflected from the material surface is partially polarized. Thus, the polarization state of the reflected light can be represented as a sum of a completely polarized component and a completely unpolarized component [5], [13]. When the completely polarized component is polarized perpendicular to the reflection surface, the wire grid parallel to the specular plane receives maximum light intensity while the wire grid perpendicular to the specular plane receives minimum light intensity. The minimum light intensity received by the wire grid is due to the partial transmission of the unpolarized component of the reflected light. The unpolarized component consists of the diffuse reflection and also the portion of the specular reflection which is unpolarized.

The difference between the maximum transmitted intensity and the minimum transmitted intensity given by (7) and (8) shows the amount of reflected light that is completely polarized. The minimum transmitted radiance $I_{\text{min}}$ is one half of the magnitude of the unpolarized light reflected from the object surface. The degree of polarization is the ratio of intensity of the perfectly polarized light reflected to the total intensity of the reflected light. If $I_p(x,y)$ is the partial polarization component and $I_{\text{all}}(x,y)$ is the total reflected component then

$$I_p(x,y) = T_p^{-1}A(x,y) = T_p^{-1}[I_{\text{max}}(x,y) - I_{\text{min}}(x,y)]$$
$$I_{\text{all}}(x,y) = I_p(x,y) + T_n^{-1}B(x,y) = T_p^{-1}[I_{\text{max}}(x,y) - I_{\text{min}}(x,y)] + 2T_p^{-1}I_{\text{min}}(x,y) = T_p^{-1}[I_{\text{max}}(x,y) + I_{\text{min}}(x,y)].$$

(16)

The degree of polarization is then obtained from (16):

$$DOP = \rho(x,y) = \frac{I_p(x,y)}{I_{\text{all}}(x,y)} = \frac{I_{\text{max}}(x,y) - I_{\text{min}}(x,y)}{I_{\text{max}}(x,y) + I_{\text{min}}(x,y)}.$$  

Equation (17) also indicates the portion of the reflected light which is completely polarized to the total amount of reflected light, denoting the partial polarization [5]. Equation (17) has a maximum value of 1 and a minimum value of 0. At a value of 0 the reflected light is completely unpolarized; thus, the diffuse component of the reflection dominates over the specular component. At the maximum value of 1, the reflected light is completely polarized, thus the specular component of the reflection dominates over the diffuse component.

The transmitted intensities are obtained using the measurement setup shown in Fig. 6. The degree of polarization obtained for the polarization sense region 1 and 2 is shown in Fig. 8.

<table>
<thead>
<tr>
<th>Region 1</th>
<th>Region 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plastic</td>
<td>Al</td>
</tr>
<tr>
<td>DOP (Max)</td>
<td>0.867</td>
</tr>
<tr>
<td>DOP (Min)</td>
<td>0.09</td>
</tr>
</tbody>
</table>

The maximum and minimum values of the DOP for the two reflecting surfaces of plastic and aluminum in the two polarization sense regions 1 and 2 are given in Table IV.

The degree of polarization is higher for plastic than for aluminum. It is observed from Fig. 8 that for plastic the maximum DOP is near 1 in both polarization sense regions, while for aluminum the maximum DOP in both polarization sense regions is less than 0.2. A higher DOP indicates higher amount of the reflected light being polarized, as stated in Section II-B that non metallic surfaces polarize the reflected light stronger than metallic surfaces.

It is further observed from Fig. 8 that as the specular angle of incidence is increased; the DOP tends to decrease for both plastic and aluminum. However, after a certain specular angle of incidence, the DOP of aluminum continues to fall but the DOP of the plastic shows a sharp rise. From (2) it is seen that $R_s$ never vanishes but $R_p$ becomes zero when

$$\tan(\varphi + \eta) = \infty$$
$$\varphi + \eta = \frac{\pi}{2}.$$  

(18)

From (18)

$$\sin \eta = \sin \left(\frac{\pi}{2} - \varphi \right)$$
$$\tan \varphi = n.$$  

(19)

where $\eta$ is the index of refraction. When the angle of incidence satisfies the condition in (19), the electric field amplitude in the reflected wave has no component which lies in the plane of incidence, meaning that the entire component $R_p$ gets refracted. The only component in the reflected wave is the one that is perpendicular to the plane of incidence. The reflected wave is completely polarized.
The angle of incidence \( \phi \) is known as the Brewster angle. The Brewster angle for plastics is near 60\(^\circ\), which explains the sharp rise of the DOP of plastic around 60\(^\circ\). For light absorbing material like metals \( R_p \) is never 0 and thus no such sharp increase in the DOP of aluminum is observed.

**D. Material Classification Using the Polarization Fresnel Ratio**

The Polarization Fresnel Ratio (PFR) is the ratio of the perpendicular Fresnel coefficient to the parallel Fresnel coefficient. Wolff in [5] introduces the PFR based on Fresnel reflectance model as a metric tool to classify materials into metals and dielectrics. The Fresnel reflection and transmission coefficients in the Fresnel reflectance model are given by (2). The theoretical Fresnel reflection coefficients for aluminum and plastic are shown in Fig. 9. The Fresnel reflection coefficient for aluminum is near 1, while that for plastic varies over the entire span from 0 to 1 for different specular angles of incidence.

The Fresnel reflection coefficient \( R_p \) is 0 near the Brewster angle for plastic and thus the PFR for dielectric (plastic) can become arbitrarily large, while the PFR for metals is limited. For the electromagnetic visible spectrum from 400 to 700 nm, it has been reported that the PFR for metals usually remains below 2 for most specular angles of incidence [5].

The PFR can be derived from (7) and (8) as

\[
R_q(x,y) = \frac{[I_{\text{max}}(x,y) - T_n I_d(x,y)]}{T_p I_q(x,y)} R_p(x,y) + R_q(x,y) \]

\[
R_p(x,y) = \frac{[I_{\text{min}}(x,y) - T_n I_d(x,y)]}{T_p I_q(x,y)} R_p(x,y) + R_q(x,y). \tag{20}
\]

Dividing (20) and (21), we get

\[
\frac{R_q(x,y)}{R_p(x,y)} = \frac{[I_{\text{max}}(x,y) - T_n I_d(x,y)]}{[I_{\text{min}}(x,y) - T_n I_d(x,y)]}. \tag{21}
\]

The specular component of reflection in metals is greater than the diffuse component of reflection \( I_d(x,y) \gg I_d(x,y) \) [9].

Thus, the diffuse component of reflection \( I_d(x,y) \) in (22) can be neglected resulting in

\[
\frac{R_q(x,y)}{R_p(x,y)} \approx \frac{I_{\text{max}}(x,y)}{I_{\text{min}}(x,y)}. \tag{23}
\]

Equation (23) is the polarization Fresnel ratio as described in [5]. In the case of dielectrics, the Fresnel reflection coefficient \( R_p \) is very small for all specular angles of incidence, and is almost 0 near the Brewster angle. The PFR for dielectrics thus can be arbitrary large as predicted by (23). For dielectrics with specular angle of incidence very close to the Brewster angle, (23) becomes

\[
\frac{R_q(x,y)}{R_p(x,y)} \gg \frac{I_{\text{max}}(x,y)}{I_{\text{min}}(x,y)}. \tag{24}
\]

A material with significant conductivity will have a significantly reduced PFR over a large range of specular angle of incidence. Since the conductivity of metals is higher than the conductivity of dielectrics, the PFR for metals is much smaller compared to that of dielectrics. As in metals the specular component of reflection is larger than the diffuse component of the reflection, the Fresnel coefficients satisfy \( R_q(x,y) \approx R_p(x,y) \) [13]. Using this condition in (5) and (6) we get \( A(x,y) \ll B(x,y) \) which from (7) and (8) means \( I_{\text{max}}(x,y) \approx I_{\text{min}}(x,y) \); thus, the PFR from (23) is nearly equal to 1 for all angles of incidence.

The \( I_{\text{max}}(x,y) \) and \( I_{\text{min}}(x,y) \) values are determined using the same measurement setup shown in Fig. 6. For varying transmission axis of the external linear polarizer, the pixel outputs averaged over 30 frames at the 0\(^\circ\) and 90\(^\circ\) polarization sensitive pixels are stored. The transmittance is computed by normalizing the output at 0\(^\circ\) and 90\(^\circ\) by the intensity at the intensity sensitive pixel in polarization sense region 1 and 2. The PFR is then calculated from the maximum and minimum transmittance. The experimentally obtained PFRs for aluminum and plastic in the polarization sense regions 1 and 2 are shown in Fig. 10.

There is a clear threshold in the PFR values for metals and dielectrics. The PFR for aluminum is in the range of 0.8 to 1 for all specular angles of incidence while the PFR for dielectrics rapidly increases near the Brewster angle. Theoretically, for a specular angle of incidence greater than the Brewster angle, the PFR for aluminum is always smaller than 2 [5]. A PFR value of
nearly 2 can be considered to belong to a dielectric. The PFR computations using the polarization sense regions 1 and 2 offer a good match to the theoretical studies and thus can be used to classify the materials into metals and dielectrics.

E. Material Classification Using the Stokes Parameters

As stated in Section II-C, the polarization state of an electromagnetic wave can be conveniently described by a set of Stokes parameters. To the best knowledge of the authors, there is no reference available on using Stokes parameters to classify materials. Here, we use the degree of polarization and linear degree of polarization obtained from the Stokes vector to classify materials into metals and dielectrics.

The measurement setup is the same as shown in Fig. 6. The outputs of the pixels sensitive to 90° and 0° are averaged over 30 frames. Simultaneously, the output of the intensity sensitive pixels with no metal grid is also recorded for varying transmission axis of the external linear polarizer. The pixel output of the 0° and 90° polarization sensitive pixels are then normalized with the output of the intensity sensitive pixels. The normalized outputs correspond to $E_{\phi 0}$ and $E_{\varphi 0}$ in (10). The degree of linear polarization is calculated using (12).

The Stokes parameters $S_0$ and $S_1$ can be obtained using (10). The degrees of linear polarization in the regions 1 and 2 are shown in Fig. 11. The Stokes degree of linear polarization for plastic has a maximum value of 1 and is higher than that for aluminum. It is further observed that the Stokes degree of linear polarization for plastics steadily decreases until it reaches the Brewster angle where the degree of polarization again increases to its maximum value. The maximum Stokes degree of linear polarization for aluminum obtained in the sense regions 1 and 2 are 0.25 and 0.38 respectively.

The degree of linear polarization for aluminum is low compared to plastic for all specular angle of incidence. Furthermore, the degree of linear polarization of plastic is found to decrease with the increase of the specular angle of incidence and a sharp rise in the degree of linear polarization is observed around the Brewster angle for plastics.

The above discussion was related to the degree of linear polarization obtained from the Stokes parameters. The Stokes degree of polarization is given by (11). The fourth Stokes parameter $S_3$ is usually ignored for natural light [11], since the phase information between orthogonally polarized light is difficult to calculate for natural light. Thus, (11) can be modified with $S_3 = 0$ as

$$DOP = \delta = \frac{S_0 + S_1}{S_0}. \quad (25)$$

$S_0$ and $S_1$ are the same as for the linear degree of polarization. $S_3$ is calculated from (10). $\nabla \varphi$, the phase difference in (10), is set to the specular angle of incidence.

The obtained degrees of polarization in the polarization sense regions 1 and 2 are shown in Fig. 12.

The plastic shows the similar response to Fig. 11 while the metal shows a steady decrease from the maximum value to minimum with increasing angle of linear polarizer. As the angle of specular incidence approaches the Brewster angle, the degree of polarization in case of plastics increases to its maximum value while no such behavior is observed for aluminum neither in sense region 1 nor in region 2. A threshold can be applied to the Brewster angle to classify between aluminum and plastic using the degree of polarization computed using the Stokes parameters.

F. Metal Classification Using the PFR

The Fresnel reflection theory can also be used to classify among conductive metallic surfaces. The Fresnel reflection coefficients depend on the index of refraction $\varepsilon$ and the specular angle of incidence $\varphi$ as shown in (2). The index of refraction $\varepsilon$ is considered to be a complex number:

$$\varepsilon = n - i\kappa \quad (26)$$

where $n$ is the simple index of refraction while $\kappa$ is called coefficient of extinction. $\kappa$ is a measure of how well a particular material scatters and absorbs electromagnetic waves. A material with low $\kappa$ allows for easy transmission of the electromagnetic waves and vice versa. The index of refraction for dielectrics is a real number as the coefficient of extinction is negligible and thus neglected, while the index of refraction for metals is a complex number. The components of the index of refraction $n$ and $\kappa$ are related to electromagnetic physical parameters of a material surface [15] as

$$n^2 = \frac{\nu \gamma c^2}{2 \left[ 1 + \sqrt{1 + \left( \frac{\lambda \sigma}{2 \pi c \gamma} \right)^2} \right]} \quad (27)$$
Among the selected three metallic surfaces, the conductivity of copper \((0.596 \times 10^7 \text{ S/cm})\) is the highest and aluminum \((0.377 \times 10^7 \text{ S/cm})\) is more conductive than zinc \((0.166 \times 10^7 \text{ S/cm})\). The higher conductivity of copper produces higher Fresnel reflection coefficients which in turns results in lower PFR, seen in the experimentally obtained PFR in both polarization sense region 1 and 2 in Fig. 13. The zinc being the less conductive should have higher PFR, as seen in polarization sense region 2. In polarization sense region 1 zinc shows lower PFR than aluminum, which could be the result of the variations in the specular angle of incidence\(^1\) of the light source. However, we still see a clear distinction between the degrees of polarization for copper, zinc, and aluminum, and the PFR values are less than 2 as stated in [5].

To extend the study of changes in the PFR with conductivity, more metallic surfaces were selected and the experimentally obtained PFR are correspondingly shown in Fig. 14.

The lower conducting metals such as steel, hibrite, hilan, and nicor show higher PFR values in both the polarization sense regions 1 and 2, compared to highly conductive metals such as copper, zinc, and nickel. The higher PFR for low conduction materials is due to the reduced reflection and lower Fresnel reflection coefficients. A clear distinction can be observed among the PFR values of various test metal surfaces of varying conductivity.

The DOP of highly conductive materials is lower than the DOP of low conducting materials. The DOP introduced in Section III-C was also calculated for various metallic surfaces and the obtained DOP in the polarization sense regions 1 and 2 is shown in Fig. 15. The resultant plots shows similar behavior as the PFR plots.

It is observed that the DOP of metal surfaces varies between 0 and 0.25 in both the polarization sense region 1 and 2. The lower conducting metal surfaces, such as steel and its varieties occupy the higher band of the range while the lower band is occupied by highly conducting metal surfaces.

There is however a difference in behavior in the two polarization sense regions for both the PFR and DOP measurements as seen in the Figs. 14 and 15. In region 2, the difference between the copper and other conducting materials is more pronounced.

\(^1\)The specular angle of incidence of the light source was not well controlled.
The transmitted intensities of the reflected light were measured for a single angle of incidence of the light ray. The measurement of the PFR at each pixel is not very accurate when the diffuse component of the reflection dominates over the specular component, in such scenario the measurement of the reflected transmitted intensities for varying angle of incidence of the light ray would serve to increase the resolution and the sensitivity of the PFR measurement.

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